



# ECI MATH

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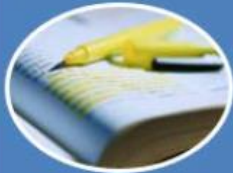
KENT O. MCINTOSH

SENIOR INDUSTRIAL-WASTE INSPECTOR (RETIRED)

# Agenda

- Introduction
  - Presentation
  - Time permitting, more “live” examples
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# Your Path to Certification



## Explore & Learn

Read Your Candidate Handbook & Study Guide, Begin gathering your documentation



## Assess Your Knowledge, Skills & Abilities

Review the KSAs and determine your areas of strength and weakness. Identify knowledge gaps you need to fill.



## Identify Resources to Fill Your KSA Gaps

Books, workshops, local sections training, CWEA state training, youtube, community colleges



## Attend a Cert Prep Session

Learn what to expect at the test site, resources to tap into and helpful hints/tools, take a sample test



## Apply for Certification

Get your documentation ready and apply. You'll have 3 months to take your test once you are approved.



## Continue Studying & Take Your Exam

Prepare, study, attend more trainings, read more books. Take the test.

*Steps to help you be successful in getting CWEA certification for competency in your field*

# REFERENCES

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- This presentation (as a PDF file)
- Applied Math for Wastewater System Operators, State of Tennessee [App. Math Wastewater]
- ECI Grade 1 Study Guide, CWEA [ECI 1 Study Guide]
- ECI Grade 3 Study Guide, CWEA [ECI 2 Study Guide]
- IWI Study Manual, CWEA
- Pretreatment Facility Inspection, OWP, CSUS [PFI]

All but the last (PFI) are available for download

(<https://cwea.app.box.com/s/nizgdiv19bt3cthuxtijm2cy8irlqnvvt>)

# Equivalents & Formulas

## Conversions

3.785 L/gal  
~~28.35 g/oz~~

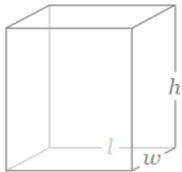
453.6 g/lb  
~~43,560 ft<sup>2</sup>/acre~~

8.34 lb/gal  
 $\pi = 3.14159$

7.48 gal/ft<sup>3</sup>

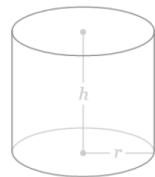
## Volumes

Rectangular Solid



$$V = lwh$$

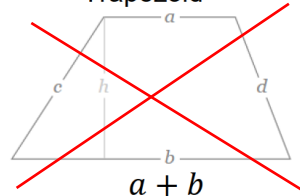
Right Cylinder



$$V = \pi r^2 h$$

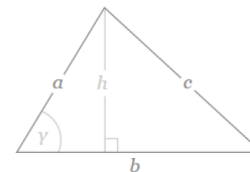
## Areas

Trapezoid



$$A = \frac{a + b}{2} h$$

Triangle



$$A = \frac{hb}{2}$$

## Formulas

Manning

$$Q = \frac{1.49 AR^{2/3} S^{1/2}}{n}$$

Q = flow rate (CFS)

A = cross-sectional area of flow (ft<sup>2</sup>)

R = hydraulic radius (ft)

S = slope of the hydraulic radius

n = Manning roughness coefficient

Counterflow  
Rinsing

$$R^n = \frac{C_p}{C_n}$$

R = rinse ratio (ratio of rinse water volumetric flow rate to the drag out volumetric flow rate)

C<sub>p</sub> = plating bath metal concentration

C<sub>n</sub> = metal concentration in the n<sup>th</sup> rinse tank

n = number of rinse tanks

Combined Waste  
Stream

$$C_T = \frac{[\sum_{i=1}^N C_i F_i] [F_T - F_D]}{[\sum_{i=1}^N F_i] [F_T]}$$

C<sub>T</sub> = alternative concentration limit

C<sub>i</sub> = concentration limit for stream i

F<sub>i</sub> = average daily flow of stream i

F<sub>T</sub> = F<sub>i</sub> + F<sub>D</sub>

F<sub>D</sub> = average daily flow of dilute wastestream

PROBABLY  
NOT  
NEEDED  
ON THE  
GRADE 1  
OR 2 TEST

# KSA 101 math

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- Recall how to calculate pH of an aqueous solution.
- Demonstrate how to balance chemical equations, identify acids and bases, and perform basic dilutions and neutralization calculations.

# Basic dilutions

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- $N = \textit{normality}$ 
  - Can be replaced with concentration
- $V = \textit{volume or flow}$

$$N_1 \times V_1 = N_2 \times V_2$$

OR

$$C_1 \times V_1 = C_2 \times V_2$$

- Normality is also a measure of concentration
- Units on both sides of eqn must be the same (N, mg/L, gpm, cfs, etc.)

# Basic dilutions, problem

---

An operator needs to make 10 gallons of a bleach dilution with a concentration 25 mg/L. The bleach on hand has a concentration of 100 mg/L. How many gallons of the concentrate must be used to achieve the dilution?

$$C_1 \times V_1 = C_2 \times V_2$$



# Basic dilutions, problem

---

An operator needs to make 10 gallons of a bleach dilution with a concentration 25 mg/L. The bleach on hand has a concentration of 100 mg/L. How many gallons of the concentrate must be used to achieve the dilution?

$$C_1 \times V_1 = C_2 \times V_2$$

$$C_1 = 25 \text{ mg/L}$$

$$V_1 = 10 \text{ gal}$$

$$C_2 = 100 \text{ mg/L}$$

$$V_2 = ?$$

# Basic dilutions, answer

---

An operator needs to make 10 gallons of a bleach dilution with a concentration 25 mg/L. The bleach on hand has a concentration of 100 mg/L. How many gallons of the concentrate must be used to achieve the dilution?

$$C_1 = 25 \text{ mg/L}$$

$$V_1 = 10 \text{ gal}$$

$$C_2 = 100 \text{ mg/L}$$

$$V_2 = ?$$

$$C_1 \times V_1 = C_2 \times V_2$$

$$V_2 = \frac{C_1}{C_2} \times V_1 = \frac{25 \text{ mg/L}}{100 \text{ mg/L}} \times 10 \text{ gal} = 2.5 \text{ gal}$$

# TRY THIS

## Basic dilutions, problem

---

What is the normality of sodium hydroxide (NaOH) solution if 25 mL of a 0.01 N sulfuric acid solution neutralizes 100 mL of the NaOH solution?

# Basic dilutions, answer

---

What is the normality of sodium hydroxide (NaOH) solution if 25 mL of a 0.01 N sulfuric acid solution neutralizes 100 mL of the NaOH solution?

$$N_1 V_1 = N_2 V_2$$

$$N_1 = \frac{V_2}{V_1} \times N_2 = \frac{25 \text{ mL}}{100 \text{ mL}} \times 0.01 \text{ N} = 0.0025 \text{ N}$$

# KSA 112 math

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- Calculate the density of liquids and which values to report, gallons that are discharged per day, and flow rate.
- Understand how to convert liquid measurements.

# KSA 116 math

- Calculate volume unit conversions.

# Density

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***Density*** — The density is the mass of a substance per unit volume. A related quantity is the specific gravity which is the density relative to water, which weights 1.0 grams/ml. A solution with a specific gravity of 1.5 would weight 1.5 grams/ml.

Units of density are g/mL, mg/L, lb/gal, etc.

# Equivalents & Formulas

## Conversions

3.785 L/gal  
~~28.35 g/oz~~

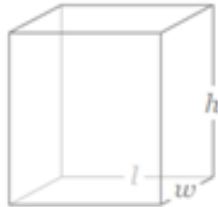
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8.34 lb/gal  
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7.48 gal/ft<sup>3</sup>

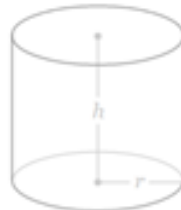
## Volumes

Rectangular Solid



$$V = lwh$$

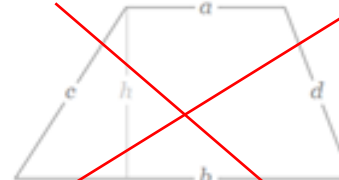
Right Cylinder



$$V = \pi r^2 h$$

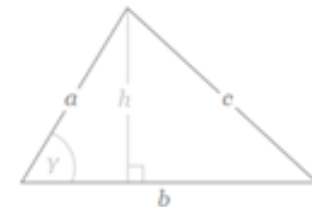
## Areas

Trapezoid



~~$$A = \frac{a + b}{2} h$$~~

Triangle



$$A = \frac{hb}{2}$$

You should also know these:

## SI PREFIXES

365 d/y

24 h/d

60 s/min

52 w/y

60 min/h

3 ft/yd

milli- (m):  $10^{-3} = 1/1000$

centi- (c):  $10^{-2} = 1/100$

kilo- (k):  $10^3 = 1000$

# Conversions

---

## Volume

- Volume is the capacity of a unit or how much it will hold
- Measured in
  - cubic units ( $\text{ft}^3$ ,  $\text{m}^3$ ,  $\text{yd}^3$ ) or
  - liquid volume units (gallons, liters, million gallons)



# Conversion, problem

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## Example 1

- Convert 1800 ft<sup>3</sup> into gallons.
- We need the conversion factor that connects the two units

$$1 \text{ cubic foot of water} = 7.48 \text{ gal}$$

- This is a ratio, so it can be written two different ways

$$\frac{1 \text{ ft}^3}{7.48 \text{ gal}} \quad \text{OR} \quad \frac{7.48 \text{ gal}}{1 \text{ ft}^3}$$

- We want to use the version that allows us to cancel out units and leave us in the units that we want

This conversion factor (7.48 gal/ft<sup>3</sup>) is provided on the Equivalents & Formulas sheet

# Conversion, answer

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Convert 1800 ft<sup>3</sup> into gallons.

7.48 gal/ft<sup>3</sup>

$$1800 \text{ ft}^3 \times \frac{7.48 \text{ gal}}{\text{ft}^3} = 13,464 \text{ gal}$$

# TRY THIS

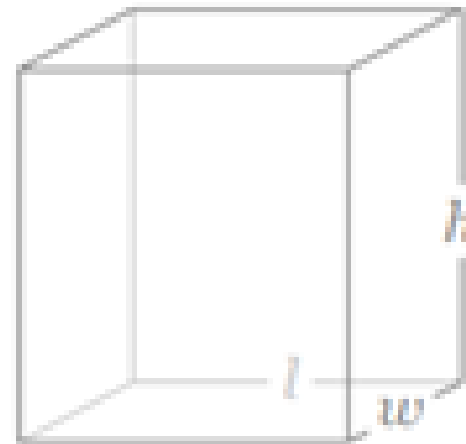
## Conversions, problem

Calculate the volume (in gallons) for a basin that measures 22 feet by 11 feet by 5 feet.

Volumes

$$V = L \times W \times H$$

Rectangular Solid



$$V = lwh$$

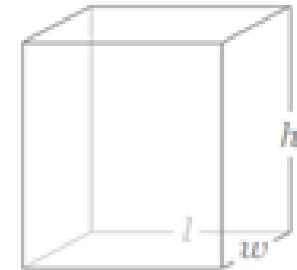
# Conversions, answer

Calculate the volume (in gallons) for a basin that measures 22 feet by 11 feet by 5 feet.

Volumes

$$\begin{aligned} V &= L \times W \times H = (22 \text{ ft})(11 \text{ ft})(5 \text{ ft}) \\ &= 1210 \text{ ft}^3 \end{aligned}$$

Rectangular Solid



$$V = lwh$$

# Conversions, answer

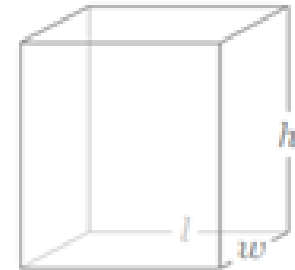
Calculate the volume (in gallons) for a basin that measures 22 feet by 11 feet by 5 feet.

Volumes

$$V = L \times W \times H = (22 \text{ ft})(11 \text{ ft})(5 \text{ ft}) \\ = 1210 \text{ ft}^3$$

$$1210 \text{ ft}^3 \times \frac{7.48 \text{ gal}}{\text{ft}^3} = 9050.8 \text{ gal}$$

Rectangular Solid



$$V = lwh$$

## KSA 106 math

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- Calculate detention time, and minimum size of an interceptor using a set of given parameters.

## KSA 201 math

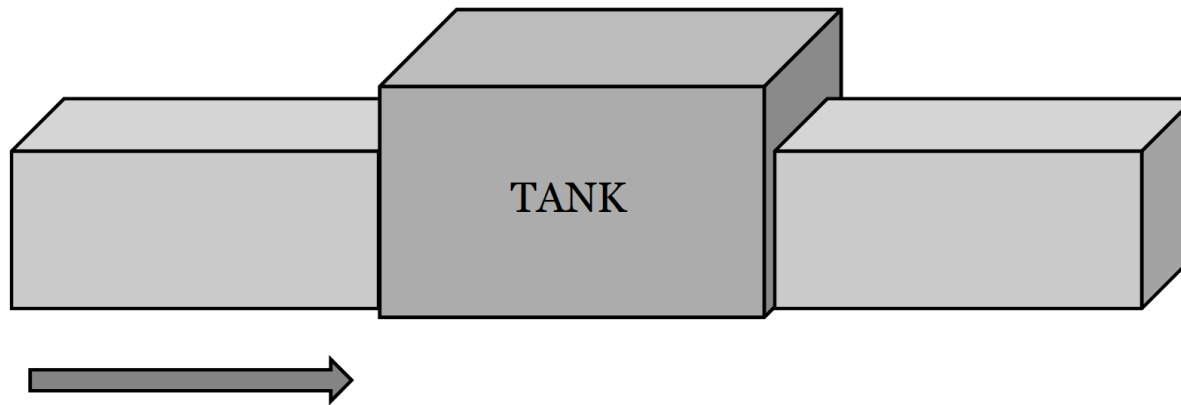
- Calculate size requirements of basin/containment structures.

## KSA 224 math

- Understand all aspects of a grease Interceptor, sizing requirements and clarifier calculations.

# Detention time

*Detention Time is Flow-Through Time*



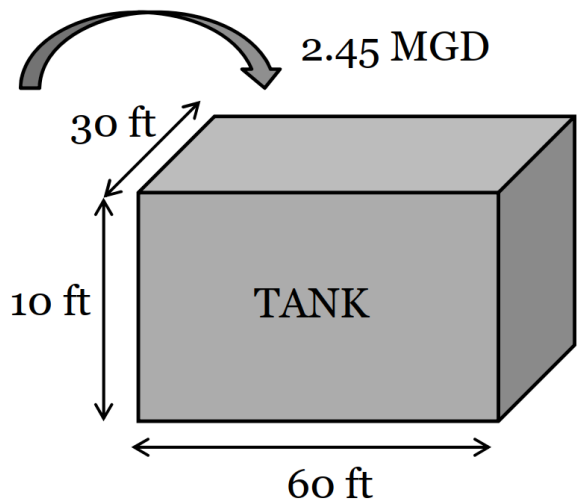
$$\text{Detention Time, hrs} = \frac{\text{Volume of Tank, gal}}{\text{Flow, gph}}$$

The equation includes a solid horizontal line with an upward-pointing arrow from the denominator to the numerator. A dashed line with an upward-pointing arrow connects the denominator to the units of the numerator.

Be sure your time and volume units match!

# Detention time, problem

The flow to a sedimentation tank 60 ft long, 30 ft wide, and 10 ft deep is 2.45 MGD. What is the detention time in the tank, in hours?



Tank Volume:

$$\text{Volume (ft}^3\text{)} = (\text{L,ft})(\text{W,ft})(\text{d,ft})$$

$$\text{Vol.} = (60\text{ft})(30\text{ft})(10\text{ft}) = 18000 \text{ ft}^3$$

$$\text{Vol.} = (18000 \text{ ft}^3)(7.48 \text{ gal/ft}^3) = 134640 \text{ gal}$$

Flow Rate:

$$\text{Flow} = \text{MGD} \rightarrow \text{gph}$$

$$= (2.45 \text{ MG/day})(1 \text{ day}/24 \text{ hrs})(1000000 \text{ gal}/1 \text{ MG})$$

$$= 102083.3333 \text{ gph}$$

$$\text{Detention Time, hrs} = \frac{\text{Volume of Tank, gal}}{\text{Flow, gph}}$$



# Detention time, answer

---

Volume = 134,640 gal

Flow  $\approx$  102,083 gph

$$\text{Detention Time, hrs} = \frac{\text{Volume of Tank, gal}}{\text{Flow, gph}}$$

$$t = \frac{V}{q} = \frac{134,640 \text{ gal}}{102,083 \text{ gal/hr}} \approx 1.32 \text{ hr}$$

# Detention time

---

You could be asked to solve for any of the three variables:

$$t = \frac{V}{q}$$

$$q = \frac{V}{t}$$

$$V = q t$$

# TRY THIS

## Detention time, problem

---

The flow to a circular clarifier is 3,940,000 gpd. If the clarifier is 75 ft in diameter and 12 feet deep, what is the clarifier detention time in hours?

$$q = 3,940,000 \text{ gpd}$$

$$V = \pi r^2 h$$

$$d = 75 \text{ ft}$$

$$h = 12 \text{ ft}$$

# Detention time, answer

---

$$q = 3,940,000 \text{ gal/d} \times \text{d}/24 \text{ hr} \approx 164,167 \text{ gal/hr}$$

$$d = 75 \text{ ft}$$

$$h = 12 \text{ ft}$$

$$V = \pi r^2 h$$

$$V = \pi r^2 h = \pi \left( \frac{d}{2} \right)^2 h = (3.14159) \left( \frac{75 \text{ ft}}{2} \right)^2 (12 \text{ ft}) \approx 53,014 \text{ ft}^3$$

$$53,014 \text{ ft}^3 \times \frac{7.48 \text{ gal}}{\text{ft}^3} \approx 396,548 \text{ gal}$$

$$t = \frac{V}{q} = \frac{396,548 \text{ gal}}{164,167 \text{ gal/hr}} \approx 2.42 \text{ hr}$$

# TRY THIS

## Containment, problem

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A company is required to construct an outdoor spill containment system. This containment area must be capable of holding double the volume of the following tanks:

- a. Square Tank 6 ft wide, 6 ft long and 6 ft high,
- b. Rectangular Tank 4 ft wide, 20 ft long and 3 ft high,
- c. Cylindrical Tank 8 ft in diameter and 9 ft high, and
- d. A 12-inch rainfall during a 24-hour period.

The company is proposing to construct a 200 foot by 200 foot level containment pad surrounded by a 15-inch wall. Will the containment system be adequate?

Ignore the “footprints” of the tanks.

# Containment, answer

Square tank:  $V_1 = 6 \times 6 \times 6 = 216 \text{ ft}^3$

Rectangular tank:  $V_2 = 4 \times 20 \times 3 = 240 \text{ ft}^3$

Cylindrical tank:  $V_3 = \pi r^2 h = \pi (d/2)^2 h = \pi (8/2)^2 (9) \approx 452 \text{ ft}^3$

$$2 \times (V_1 + V_2 + V_3) = 2(216 + 240 + 452) = 1817 \text{ ft}^3$$

Rainfall: 12 in. = 1 ft,  $1 \times 200 \times 200 = 40,000 \text{ ft}^3$

$$\text{Total} = 1817 + 40,000 = 41,817 \text{ ft}^3$$

Proposed volume: 15 in. =  $15 \text{ in.} \times \frac{1 \text{ ft}}{12 \text{ in.}} = 1.25 \text{ ft}$

$$1.25 \times 200 \times 200 = 50,000 \text{ ft}^3 > 41,817 \text{ ft}^3$$



# KSA 117 math

- Understand how to measure and calculate sewer use fees.
- 

# KSA 203 math

- Calculate Production-Based and Mass-Based limits.

# KSA 223 math

- Ability to calculate penalties for exceeding discharge limitations

# KSA 224 math

- Calculate annual sewer service fees, organic loading and wastewater strength.

# THE DAVIDSON PIE





# Davidson Pie

$$lb/d = (mg/L)(8.34)(mgd)$$

The pie can be thought of as a fraction:

$$\frac{lb / d}{mg / L \bullet 8.34 \bullet mgd}$$

## THE DAVIDSON PIE



Given any two of the three unknowns, you can solve for the third.

Quantities in the same half of the pie are multiplied together; those on opposite sides are divided.

# Davidson Pie, problem

- Lab results for MLSS = 3000 mg/L
- How many pounds of Mixed Liquor Suspended Solids are in the aeration basin if the basin volume is 2 million gallons?

$$lb = (mg/L)(8.34)(MG)$$

## THE DAVIDSON PIE



# Davidson Pie, answer

- Lab results for MLSS = 3000 mg/L
- How many pounds of Mixed Liquor Suspended Solids are in the aeration basin if the basin volume is 2 million gallons?

$$lb = (mg/L)(8.34)(MG)$$

## THE DAVIDSON PIE



$$lb = \left(3000 \frac{mg}{L}\right) (8.34)(2 MG) = 50,040 lb$$

# TRY THIS

## Davidson Pie, problem

- Lab results for TSS = 25 mg/L
- How many pounds of Total Suspended Solids are being discharged to the receiving stream if your flow is 10 MGD?

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{MGD})$$

### THE DAVIDSON PIE



# Davidson Pie, answer

- Lab results for TSS = 25 mg/L
- How many pounds of Total Suspended Solids are being discharged to the receiving stream if your flow is 10 MGD?

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{mgd})$$

$$\frac{\text{lb}}{\text{d}} = \left(25 \frac{\text{mg}}{\text{L}}\right) (8.34)(10 \text{ MGD}) = 2085 \text{ lb/d}$$

## THE DAVIDSON PIE



# Sewer-use fees, problem

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A meat packing plant discharges a waste flow of 45,000 GPD with a BOD of 3,500 mg/L and suspended solids of 1,300 mg/L. If the local POTW agency assesses the following charges, what would be the company's annual sewer service fee if the company works 260 days per year?

BOD = \$68.00 / lb BOD

SS = \$59.00 / lb SS

Flow = \$218.00 / MG

# TRY TO FIND SS FEE

PFI

722

## Sewer-use fees, answer

$q = 45,000 \text{ gpd} = 0.045 \text{ MGD}$	BOD	=	\$68.00 / lb BOD
$\text{BOD} = 3500 \text{ mg/L}$	SS	=	\$59.00 / lb SS
$\text{SS} = 1300 \text{ mg/L}$	Flow	=	\$218.00 / MG
$260 \text{ d/y}$			

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{mgd}) \quad \text{fee} = \text{lb/d} \times \text{d/y} \times \$/\text{lb}$$

$$\text{BOD} = (3500)(8.34)(0.045) \frac{\text{lb}}{\text{d}} = 1313.55 \text{ lb/d}$$

$$\text{SS} = ?$$

$$\text{Flow} = ?$$

$$\text{Annual fee} = ?$$

# TRY TO FIND FLOW FEE

PFI

722

## Sewer-use fees, answer

$q = 45,000 \text{ gpd} = 0.045 \text{ MGD}$	BOD	=	\$68.00 / lb BOD
BOD = 3500 mg/L	SS	=	\$59.00 / lb SS
SS = 1300 mg/L	Flow	=	\$218.00 / MG
260 d/y			

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{mgd})$$

$$\text{fee} = \text{lb/d} \times \text{d/y} \times \$/\text{lb}$$

$$\text{BOD} = (3500)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$68}{\text{lb}} = \$23,223,564.00$$

$$\text{SS} = (1300)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$59}{\text{lb}} = \$7,484,232.60$$

Flow = ?



# Sewer-use fees, answer

$q = 45,000 \text{ gpd} = 0.045 \text{ MGD}$	BOD	=	\$68.00 / lb BOD
BOD = 3500 mg/L	SS	=	\$59.00 / lb SS
SS = 1300 mg/L	Flow	=	\$218.00 / MG
260 d/y			

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{mgd}) \quad \text{fee} = \text{lb/d} \times \text{d/y} \times \$/\text{lb}$$

$$BOD = (3500)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$68}{\text{lb}} = \$23,223,564.00$$

$$SS = (1300)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$59}{\text{lb}} = \$7,484,232.60$$

$$Flow = (0.045 \text{ MGD}) \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$218}{\text{MG}} = \$2550.60$$

# Sewer-use fees, answer

PFI

723

$$q = 45,000 \text{ gpd} = 0.045 \text{ MGD}$$

$$\text{BOD} = 3500 \text{ mg/L}$$

$$\text{SS} = 1300 \text{ mg/L}$$

$$260 \text{ d/y}$$

$$\text{BOD} = \$68.00 / \text{lb BOD}$$

$$\text{SS} = \$59.00 / \text{lb SS}$$

$$\text{Flow} = \$218.00 / \text{MG}$$

$$\text{lb/d} = (\text{mg/L})(8.34)(\text{mgd})$$

$$\text{fee} = \text{lb/d} \times \text{d/y} \times \$/\text{lb}$$

$$\text{BOD} = (3500)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$68}{\text{lb}} = \$23,223,564.00$$

$$\text{SS} = (1300)(8.34)(0.045) \frac{\text{lb}}{\text{d}} \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$59}{\text{lb}} = \$7,484,232.60$$

$$\text{Flow} = (0.045 \text{ MGD}) \times \frac{260 \text{ d}}{\text{y}} \times \frac{\$218}{\text{MG}} = \$2550.60$$

$$\text{Total} = \$23,223,564 + \$7,484,233 + \$2551 = \$30,710,347$$

# Discharge penalty, problem

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A metal finisher has the following discharge limitations: copper, 3.0 mg/L; lead, 0.7 mg/L; chromium, 2.7 mg/L; and nickel, 3.3 mg/L. The metal finisher had the following metal concentrations in a recent 24-hour discharge sample collected and analyzed for sewer-use fees: Cu, 15.0 mg/L; Pb, 3.2 mg/L; Cr, 18.3 mg/L; and Ni, 6.3 mg/L. The metal finisher discharges a flow of 30,000 gallons per day (0.03 MGD). The sewer-use penalties in dollars per pound discharged over the limitations are: Cu, \$225/lb; Pb, \$325/lb; Cr, \$250/lb; and Ni \$375/lb. What would be the metal finisher's daily monetary penalty for exceeding the discharge limitations?

# Discharge penalty, problem

---

Cu = 15 mg/L

limit = 3 mg/L Cu

Pb = 3.2 mg/L

limit = 0.7 mg/L Pb

Cr = 18.3 mg/L

limit = 2.7 mg/L Cr

Ni = 6.3 mg/L

limit = 3.3 mg/L Ni

Q = 30,000 GPD = 0.03 MGD

## Penalties over limit

- \$225/lb Cu
- \$325/lb Pb
- \$250/lb Cr
- \$375/lb Ni

# TRY THE OTHERS

PFI

723

## Discharge penalty, answer

---

Cu = 15 mg/L

Pb = 3.2 mg/L

Cr = 18.3 mg/L

Ni = 6.3 mg/L

Q = 0.03 MGD

limit = 3 mg/L Cu

limit = 0.7 mg/L Pb

limit = 2.7 mg/L Cr

limit = 3.3 mg/L Ni

Penalties over  
limit

- \$225/lb Cu
- \$325/lb Pb
- \$250/lb Cr
- \$375/lb Ni

Cu:  $(15 - 3)(8.34)(0.03) \times \$225 = \$675.54$

Pb ?

Cr ?

Ni ?

# Discharge penalty, answer

Cu = 15 mg/L

limit = 3 mg/L Cu

Pb = 3.2 mg/L

limit = 0.7 mg/L Pb

Cr = 18.3 mg/L

limit = 2.7 mg/L Cr

Ni = 6.3 mg/L

limit = 3.3 mg/L Ni

Q = 30,000 MGD

Penalties over  
limit

- \$225/lb Cu
- \$325/lb Pb
- \$250/lb Cr
- \$375/lb Ni

$$\text{Cu: } (15 - 3)(8.34)(0.03) \times \$225 = \$675.54$$

$$8.34 \times 0.03 = 0.2502$$

$$\text{Pb: } (3.2 - 0.7)(0.2502) \times \$325 = \$203.29$$

$$\text{Cr: } (18.3 - 2.7)(0.2502) \times \$250 = \$975.78$$

$$\text{Ni: } (6.3 - 3.3)(0.2502) \times \$375 = \$281.48$$

$$\text{Total} = \$2136.08$$

# KSA 209 math

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- Understand how to calculate flow rate, and Open Channel Flow Measurement devices.

# Velocity

- The speed at which something is moving
- Measured in

○  $ft/min$   $ft/sec$   $miles/hr$  etc

$$Velocity = \frac{distance}{time}$$

This equation is NOT on the Equivalents & Formulas sheet; you should memorize it.



# TRY THIS

## Velocity, problem

---

Blue dye is placed in a sewer line at a manhole. Three (3) minutes later, the dye appears in a manhole 125 feet down stream. What is the velocity of the flow in ft/min?

$$Velocity = \frac{distance}{time}$$

# Velocity, answer

---

Blue dye is placed in a sewer line at a manhole. Three (3) minutes later, the dye appears in a manhole 125 feet down stream. What is the velocity of the flow in ft/min?

$$\text{Velocity} = \frac{\text{distance}}{\text{time}}$$

$$\text{Vel} = \frac{125 \text{ ft}}{3 \text{ min}}$$

$$\text{Vel} = 41.67 \text{ ft}/\text{min}$$

# Flow

- The volume of water that flows over a period of time
- Measured in
  - $ft^3/sec$     $ft^3/min$     $gal/day$     $MG/D$

$$Flow = (Area)(Velocity)$$

$$Q = AV$$

This equation is NOT on the Equivalents & Formulas sheet; you should memorize it.

# TRY THIS

## Flow, problem

---

Water is flowing at velocity 3 ft/sec through a channel that is 2 feet wide and 1.5 feet deep. What is the flow in cubic feet per second?

$$Q = AV$$

# Flow, answer

---

Water is flowing at velocity 3 ft/sec through a channel that is 2 feet wide and 1.5 feet deep. What is the flow in cubic feet per second?

$$Q = AV$$

$$Q = (l)(w)(velocity)$$

$$Q = (2ft)(1.5ft)(3 \text{ ft}/sec)$$

$$Q = 9 \text{ ft}^3/sec$$

The equation for the area of a rectangle (L x W) is NOT on the Equivalents & Formulas sheet; you should memorize it.

# KSA 210 math

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- Calculate and understand how to identify an illicit discharge in the sanitary sewer.

# Weighted average

---

Common example of weighted average is calculation of grade-point average:

$$GPA = \frac{\sum g_i u_i}{\sum u_i}$$

$g_i$  are the grade points (A = 4, B = 3, etc.)

$u_i$  are the number of units

# Weighted average, example

---

$$GPA = \frac{\sum g_i u_i}{\sum u_i}$$

UNITS	GRADE	POINTS	GRADE POINT
3	F	0	
2	D	1	
5	B	3	
TOTAL =			TOTAL =



# Weighted average, example

UNITS	GRADE	POINTS	GRADE POINT
3	F	0	0
2	D	1	2
5	B	3	15

# Weighted average, example

UNITS	GRADE	POINTS	GRADE POINT
3	F	0	0
2	D	1	2
5	B	3	15
10	$= \sum u_i$	$\sum g_i u_i =$	17

# Weighted average, example

UNITS	GRADE	POINTS	GRADE POINT
3	F	0	0
2	D	1	2
5	B	3	15
10	= $u_i$	$g_i =$	17

$$GPA = \frac{\sum g_i u_i}{\sum u_i} = \frac{17}{10} = 1.7 \text{ (C -)}$$

# Illicit discharge, problem

---

A plating company has an underground hard chrome waste recirculation tank located close to an underground sewer. The company's wastestream flow is 25,000 gallons per day with a chromium content of 10.5 mg/L. During routine sewer monitoring upstream and downstream of this company, the following information was obtained:

	<b>Upstream</b>	<b>Downstream</b>
Flow, GPD	150,000 GPD	175,000 GPD
Chromium Conc, mg/L	0.85 mg/L	3.2 mg/L

Could the inspector suspect a leak in the underground chromium tank migrating into the sewer system?

# Illicit discharge, answer

---

A plating company has an underground hard chrome waste recirculation tank located close to an underground sewer. The company's wastestream flow is 25,000 gallons per day with a chromium content of 10.5 mg/L. During routine sewer monitoring upstream and downstream of this company, the following information was obtained:

	<b>Upstream</b>	<b>Downstream</b>
Flow, GPD	150,000 GPD	175,000 GPD
Chromium Conc, mg/L	0.85 mg/L	3.2 mg/L

Could the inspector suspect a leak in the underground chromium tank migrating into the sewer system?

$$q_1 = 25,000 \text{ gpd}$$

$$c_1 = 10.5 \text{ mg/L}$$

$$q_2 = 150,000 \text{ gpd}$$

$$c_2 = 0.85 \text{ mg/L}$$

$$c = 3.2 \text{ mg/L}$$

# Illicit discharge, answer

---

$$q_1 = 25,000 \text{ gpd}$$

$$q_2 = 150,000 \text{ gpd}$$

$$c_1 = 10.5 \text{ mg/L}$$

$$c_2 = 0.85 \text{ mg/L}$$

$$c = 3.2 \text{ mg/L}$$

$$c = \frac{\sum c_i q_i}{\sum q_i} = \frac{(10.5 \text{ mg/L})(25,000 \text{ gpd}) + (0.85 \text{ mg/L})(150,000 \text{ gpd})}{(25,000 + 150,000) \text{ gpd}}$$
$$= \frac{262,500 + 127,500}{25,000 + 150,000} = \frac{390,000}{175,000} = 2.23 \text{ mg/L}$$

3.2 > 2.23, so there does appear to be a leak

# Weighted average, problem

---

The local municipal sewage treatment plant's effluent has a TDS averaging 600 mg/L. The flow averages 24 MGD. The maximum allowable discharge of TDS in the effluent is 750 mg/L. A new industry is proposing to locate in this town and to discharge 1.5 MGD to the sewer. The agency intends to keep the treatment plant's effluent TDS below 710 mg/L.

What is the maximum TDS concentration the new industry can discharge at the proposed 1.5 MGD flow rate?

$$c_1 = 600 \text{ mg/L}$$

$$c_2 = ?$$

$$q_1 = 24 \text{ MGD}$$

$$q_2 = 1.5 \text{ MGD}$$

$$c \leq 710 \text{ mg/L}$$

# TRY THIS

## Weighted average, answer

---

$$c_1 = 600 \text{ mg/L}$$

$$c_2 = ?$$

$$q_1 = 24 \text{ MGD}$$

$$q_2 = 1.5 \text{ MGD}$$

$$c \leq 710 \text{ mg/L}$$

$$c = \frac{\sum c_i q_i}{\sum q_i} = \frac{c_1 q_1 + c_2 q_2}{q_1 + q_2}$$



# Weighted average, answer

---

$$c_1 = 0 \text{ mg/L}$$

$$c_2 = X$$

$$q_1 = 24 \text{ MGD}$$

$$q_2 = 1.5 \text{ MGD}$$

$$c \leq 710 \text{ mg/L}$$

$$c = \frac{\sum c_i q_i}{\sum q_i} = \frac{c_1 q_1 + c_2 q_2}{q_1 + q_2}$$

$$710 = \frac{(600)(24) + (X)(1.5)}{24 + 1.5}$$

**SOLVE FOR X**

# Weighted average, answer

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$$710 = \frac{(600)(24) + (X)(1.5)}{24 + 1.5}$$

$$1.5X + 14,400 = 710(24 + 1.5)$$

$$X = \frac{710(25.5) - 14,400}{1.5} = 2470 \text{ mg/L}$$

# QUESTIONS?

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